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## PRELIMINARY <br> PHYSICS <br> SIGMA <br> SCIENCE <br> Q\&A

## Week 2: Collisions I

Question 1 (3 marks)
An object of mass 100 kg travelling at $12 \mathrm{~ms}^{-1}$ collides with a stationary object of 220 kg . If these objects stick together, determine the initial velocity of the wreckage.


## Worked solution:

Law of conservation of momentum states that $\Delta \mathrm{p}=0$.
$\therefore \mathrm{p}_{\mathrm{i}}=\mathrm{p}_{\mathrm{f}}$
Assigning object 1 to the 100 kg mass and object 2 to the 220 kg mass, we end up with:

$$
\mathbf{m}_{1} \mathbf{u}_{1}+\mathbf{m}_{2} \mathbf{u}_{2}=\mathbf{m}_{1} \mathbf{v}_{\mathbf{1}}+\mathbf{m}_{2} \mathbf{v}_{\mathbf{2}}
$$

HOWEVER, seeing as the objects stick together, they both move with the same velocity after the collision, hence:

$$
\begin{gathered}
\mathbf{m}_{1} \mathbf{u}_{1}+\mathbf{m}_{2} \mathbf{u}_{\mathbf{2}}=\left(\mathbf{m}_{1}+\mathbf{m}_{\mathbf{2}}\right) \mathbf{v} \\
(100 \times 12)+(220 \times 0)=(100+220) v \\
\therefore v=\frac{(100 \times 12)+(220 \times 0)}{(100+220)}=3.75 \mathrm{~ms}^{-1}
\end{gathered}
$$

in the same direction as the initial velocity of the 100 kg mass (Right)

Question 2 (3 marks)
An object of mass 150 kg travelling at $12 \mathrm{~ms}^{-1}$ collides with an object of mass 275 kg travelling at the same speed in the opposite direction. If these objects stick together, determine the initial velocity of the wreckage.


## Worked solution:

Law of conservation of momentum states that $\Delta \mathrm{p}=0$.
$\therefore \mathrm{p}_{\mathrm{i}}=\mathrm{p}_{\mathrm{f}}$
Assigning object 1 to the 150 kg mass and object 2 to the 275 kg mass, we end up with:

$$
\mathbf{m}_{1} \mathbf{u}_{1}+\mathbf{m}_{2} \mathbf{u}_{2}=\mathbf{m}_{1} \mathbf{v}_{\mathbf{1}}+\mathbf{m}_{2} \mathbf{v}_{\mathbf{2}}
$$

HOWEVER, seeing as the objects stick together, they both move with the same velocity after the collision, hence:

$$
\mathbf{m}_{1} \mathbf{u}_{1}+\mathbf{m}_{2} \mathbf{u}_{2}=\left(\mathbf{m}_{1}+\mathbf{m}_{2}\right) \mathbf{v}
$$

Seeing as they are moving in opposite directions, we must note that one of the objects must have a negative initial velocity. By convention, left is defined as negative and hence we will define the 275 kg as having a negative initial velocity.

$$
\begin{aligned}
& (150 \times 12)+(275 \times-12)=(150+275) v \\
& \therefore v=\frac{(150 \times 12)+(275 \times-12)}{(150+275)}=-3.5 m s^{-1}
\end{aligned}
$$

$\therefore v=3.5 \mathrm{~ms}^{-1}$ in the same direction as the 275 kg objects initial motion (Left)

Question 3 (3 marks)
An object of mass 100 kg travelling at $35 \mathrm{~ms}^{-1}$ collides with an object of mass 220 kg travelling at $12 \mathrm{~ms}^{-1}$ in the same direction as the 100 kg mass. After the collision, the 220 kg object gains $2 \mathrm{~ms}^{-1}$, determine the final velocity of the 100 kg mass.



## Worked solution:

Law of conservation of momentum states that $\Delta \mathrm{p}=0$.
$\therefore \mathrm{p}_{\mathrm{i}}=\mathrm{p}_{\mathrm{f}}$
Assigning object 1 to the 100 kg mass and object 2 to the 220 kg mass, we end up with:

$$
\mathbf{m}_{1} \mathbf{u}_{1}+\mathbf{m}_{2} \mathbf{u}_{2}=\mathbf{m}_{1} \mathbf{v}_{\mathbf{1}}+\mathbf{m}_{2} \mathbf{v}_{2}
$$

These objects MAY NOT stick together, so we cannot reduce it to the equation which we used in questions $2 \& 3$.

$$
\begin{gathered}
(100 \times 35)+(220 \times 12)=100 v_{1}+(220 \times(12+2)) \\
\therefore v_{1}=\frac{(100 \times 35)+(220 \times 12)-(220 \times 14)}{100}=30.6 \mathrm{~ms}^{-1}=31 \mathrm{~ms}^{-1}\left(2 \mathrm{sf} f^{*}\right) R \mathrm{Right}
\end{gathered}
$$

* Note:
- ambiguity exists in number of sig figs in 100 , but most teachers hate 1 sf.

